### 

### Semester One Examination, 2022

### Question/Answer booklet

# MATHEMATICS METHODS

**UNIT 3**

## Section One:

## Calculator-free

|  |  |
| --- | --- |
| **Your Name:** |  |
| **Your Teacher’s Name:** |  |

## Time allowed for this section

Reading time before commencing work: five minutes

Working time: fifty minutes

## Materials required/recommended for this section

***To be provided by the supervisor***

This Question/Answer booklet

Formula sheet

***To be provided by the candidate***

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

## Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Question | Marks | Max | Question | Marks | Max |
| 1 |  | 8 | 5 |  | 6 |
| 2 |  | 10 | 6 |  | 13 |
| 3 |  | 8 |  |  |  |
| 4 |  | 8 |  |  |  |

**Structure of this paper**

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Section | Number of questions available | Number of questions to be answered | Working time (minutes) | Marks available | Percentage of examination |
| Section One:  Calculator-free | 6 | 6 | 50 | 53 | 35 |
| Section Two:  Calculator-assumed | 10 | 10 | 100 | 100 | 65 |
|  |  |  |  | **Total** | 100 |

**Instructions to candidates**

1. The rules for the conduct of the Western Australian Certificate of Education ATAR course examinations are detailed in the *Year 12 Information Handbook 2019*. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer booklet.
3. You must be careful to confine your answers to the specific questions asked and to follow any instructions that are specific to a particular question.
4. Additional pages for the use of planning your answer to a question or continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number.
5. **Show all your working clearly.**Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you **do not use pencil**, except in diagrams.
7. The Formula sheet is **not** to be handed in with your Question/Answer booklet.

**Section One: Calculator-free (53 marks)**

This section has **six** questions. Answer **all** questions. Write your answers in the spaces provided.

Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.

● Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.

● Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.

Working time: 50 minutes.

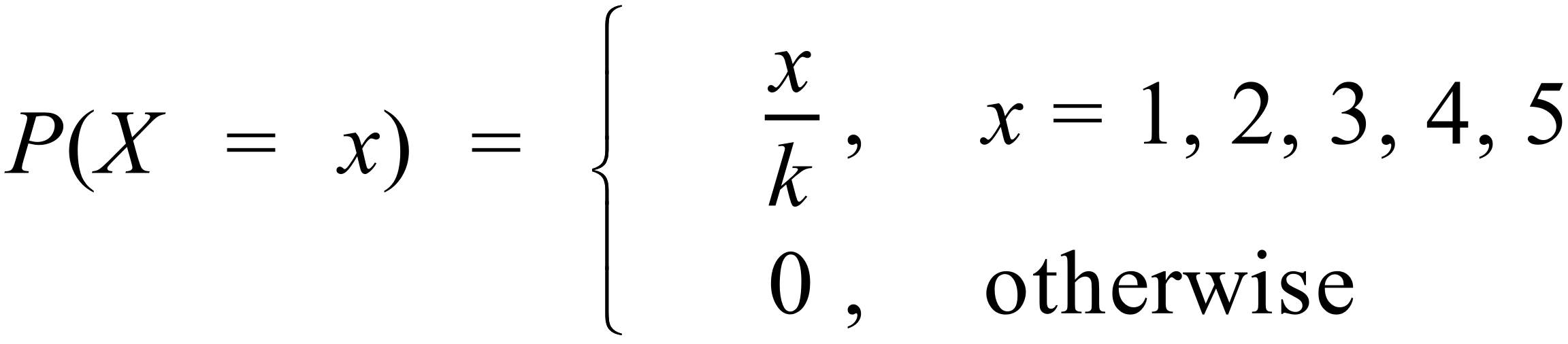
Question 1 (8 marks)

The function is defined for by , and .

1. Show that (2 marks)
2. Determine the coordinates and nature of all stationary points of . Justify your answer. (4 marks)
3. Show that has no points of inflection. (2 marks)

**Question 2 (10 marks)**

The discrete random variable has a probability function with



(a) Determine the value of (2 marks)

Determine:

(b) (i) (2 marks)

(ii) (2 marks)

(c) A second discrete random variable is defined to be

If and the standard deviation of is, determine and . (4 marks)

Question 3 (8 marks)

<EFOFEX>
id:fxd{ff8b9e87-281b-4421-9a2e-8ead16b06f94}

FXData:
</EFOFEX>The graph of between  
 and is shown at right.  
  
Approximate values for and   
are and respectively.

(a) Use the areas of the rectangles shown to explain why . (3 marks)

(b) Evaluate . (3 marks)

(c) Evaluate . (2 marks)

Question 4 (8 marks)

A student observes the graphs of three binomial distributions with the assigned random variables and for each graph. For all three distributions, the value of is constant, but the values of are 0.25, 0.5 and 0.9 respectively.

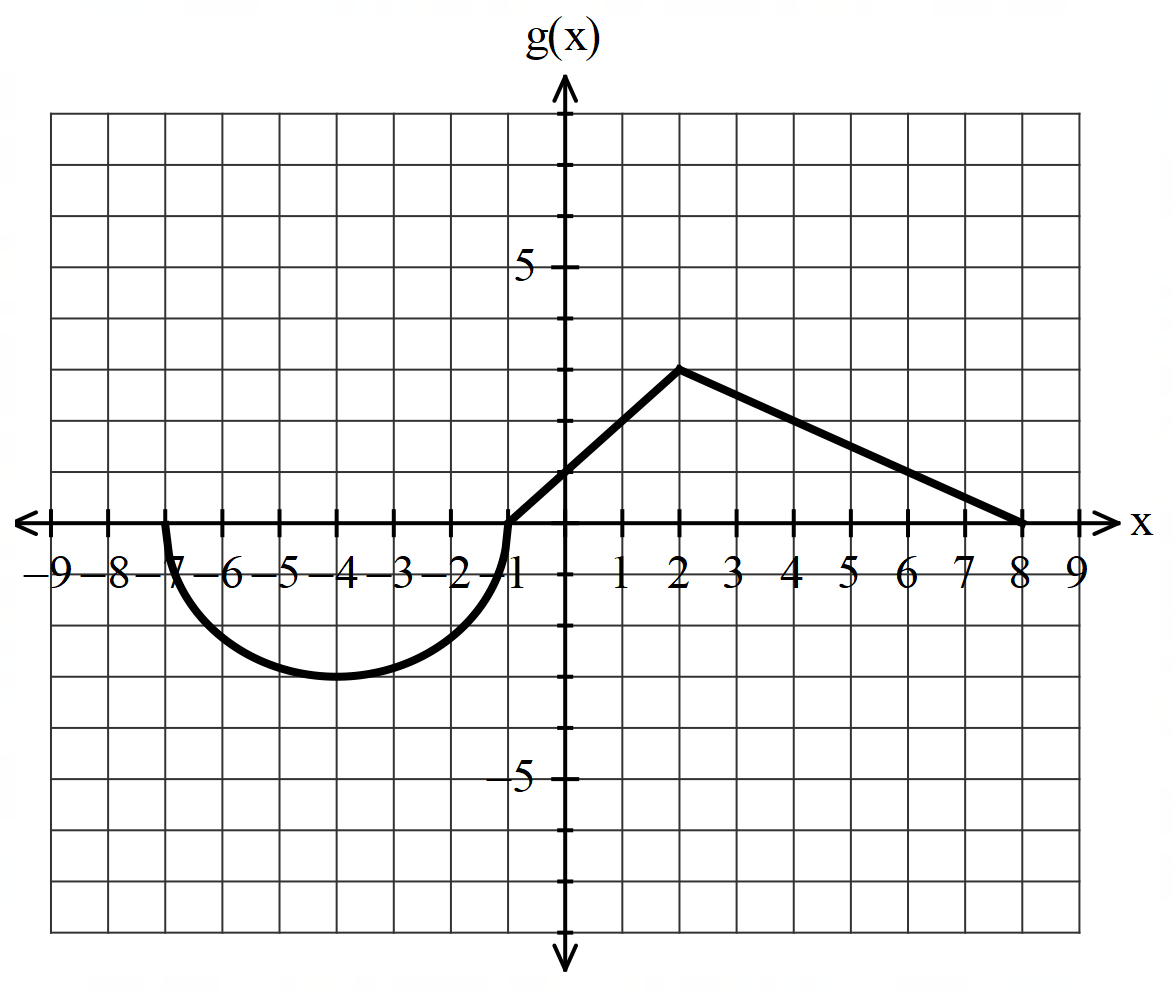
1. The student notes that one of the distributions produced a graph that is skewed to the right (long tail to the right). Which of the values of were used to produce this graph? Give justification for your choice. (2 marks)
2. The standard deviation when is 6. Determine the value of . (3 marks)
3. Using your answer from part b), show how to calculate the following without the use of a calculator. Do not evaluate your answer.
   1. (1 mark)
   2. (2 marks)

**Question 5 (6 marks)**

1. Determine (2 marks)
2. Hence, evaluate the following in exact form: (4 marks)

**Question 6 (13 marks)**

The graph of is given as below, which consists of a semi-circle for and a triangle for



Given that , where .

1. Determine the intervals where is increasing and decreasing, respectively.

(2 marks)

1. Determine the intervals where is concave up and concave down, respectively.

(2 marks)

1. Determine the value(s) of when reaches any stationary point(s) and the nature of the stationary point(s), if any. (2 marks)
2. Determine the exact values of . (2 marks)

1. Determine the exact values . (2 marks)
2. Sketch the graph of in the axes provided below, for Label key features. (3 marks)

Chart, scatter chart

Description automatically generated

Additional working space

Question number: \_\_\_\_\_\_\_\_

Additional working space

Question number: \_\_\_\_\_